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Dynamic Programming for Energy State Control of Machine Tools in Manufacturing with Part Admission Control

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SMMSO 2017

Date: June 6th, 2017

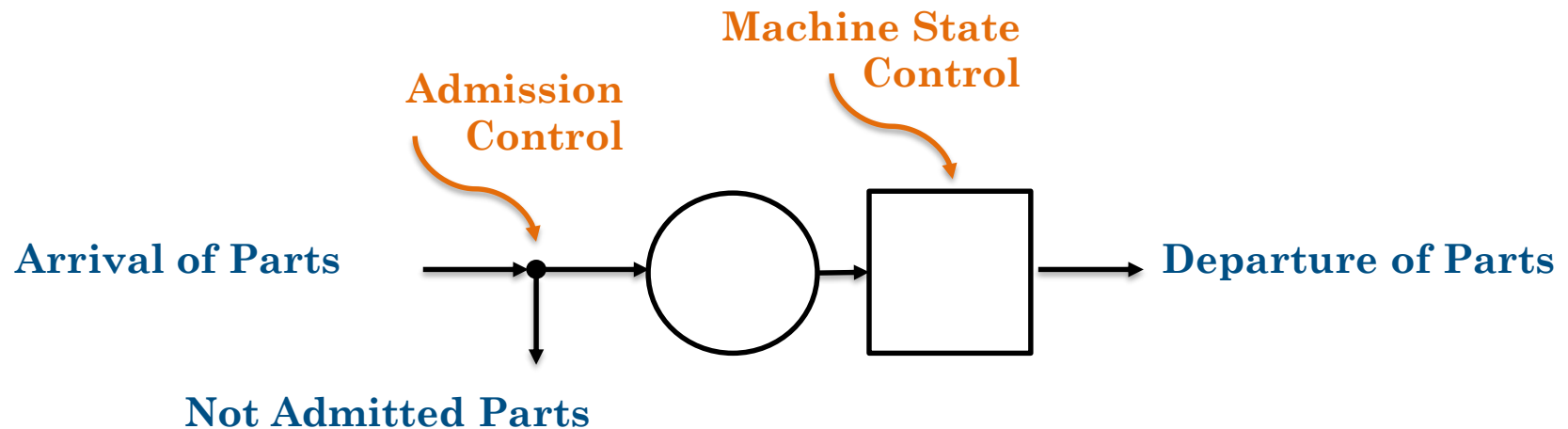
- **Introduction and State of the Art**
- **Assumptions**
- **DP Model**
- **Numerical Results**
- **Conclusions and Future Developments**

This work focuses on the combined problem of:

- Controlling the switching off/on of machine tool for energy saving purposes;
- Controlling the admission of parts;

using buffer occupancy information from the upstream buffer.

The problem is to dynamically control the system so as to minimize discounted cost.



- The **control of admission** aims at **reducing the congestion** (in the form of jobs waiting in the buffer) in a system.
- A cost incurs whenever a customer is rejected (or, equivalently, a reward is earned whenever a customer is accepted).
- Problems of this type have been studied in the literature (e.g. [1] [2] [3][4]) and it is shown that threshold policies are optimal.
- Also finite capacity systems can be modeled by increasing the holding cost when the queue length reaches the capacity.

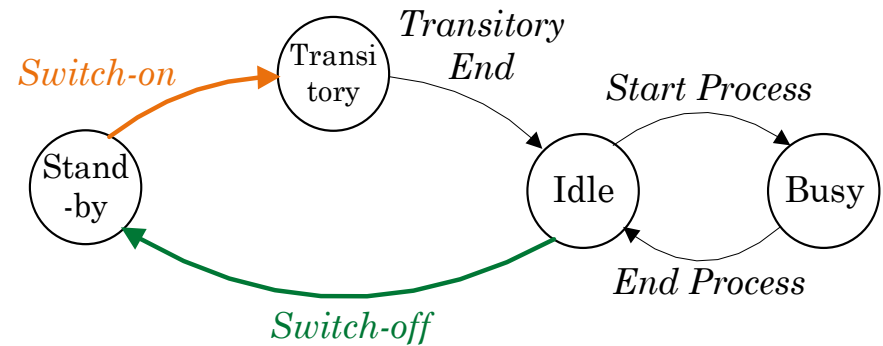
[1] Serfozo, R.: Optimal control of random walks, birth and death processes, and queues. Adv. Appl. Probab. 13, 61–83 (1981)

[2] Stidham, S.: Optimal control of admission to a queueing system. IEEE Trans. Autom. Control 30, 705–713 (1985)

[3] Stidham, S., Weber R.: A survey of Markov decision models for control of networks of queues. Queueing Systems, 13(1), 291–314, 1993

[4] Jain, A. and Lim, A. E. B., Shanthikumar, J. G.: On the optimality of threshold control in queues with model uncertainty. Queueing Systems, 65(2), 157–174 (2010)

- The **control of machine states** for energy saving aims at **reducing the amount of energy required when the machine is not working on parts (idle)**.
- The service is interrupted and resumed based on **time** information or on the **buffer level** information.
- Vacation queueing theory, Dynamic Programming, Simulation, ...



[5] M. Yadin and P. Naor. Queueing systems with removable service station. *Operational Research Quarterly* 14, pages 393–405, 1963.

[6] M. Mashaei and B. Lennartson. Energy Reduction in a Pallet- Constrained Flow Shop Through On/Off Control of Idle Machines. *Automation Science and Eng., IEEE Trans. on*, 10(1):45–56, January 2013

[7] Q. Chang, G. Xiao, S. Biller, and L. Li. Energy Saving Opportunity Analysis of Automotive Serial Production Systems (March 2012). *Automation Science and Eng., IEEE Trans. on*, 10(2):334–342, April 2013.

[8] Frigerio, N., A. Matta. 2016. Analysis on Energy Efficient Switching of Machine Tool With Stochastic Arrivals and Buffer Information. *Automation Science and Engineering, IEEE Transactions on* 13(1) 238–246.

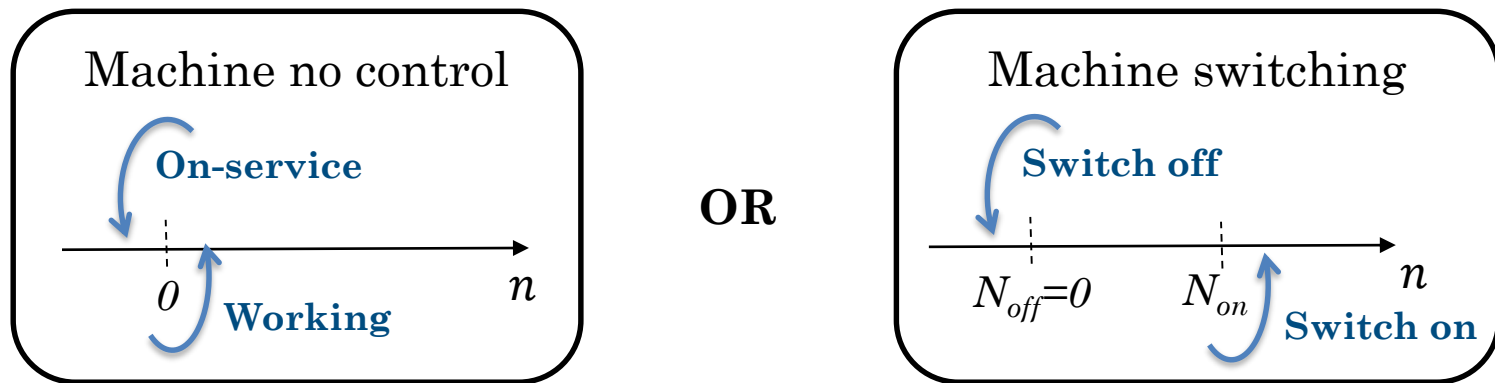
[9] Z. Jia, L. Zhang, J. Arinez, and G. Xiao. Performance Analysis of Bernoulli Serial Production Lines with Switch-On/Off Machine Control. *IEEE Conf. of Automation Science and Eng.*, August 24–28 2015.

[10] Frigerio N. 2016. Optimal Stochastic Switching of Machine Tools in Energy Efficient Manufacturing Systems, PhD Thesis, Politecnico di Milano, Italy.

The objective is to minimizing total discounted cost with:

- Machine energy cost $c(x)$ with $x =$ machine state;
- Inventory holding cost $h(n)$ where $h(\cdot)$ is convex on number of parts n ;
- Production reward $r \geq r_{\min}$ earned at process completion.

The **optimal policy** is an **exhaustive service discipline**:

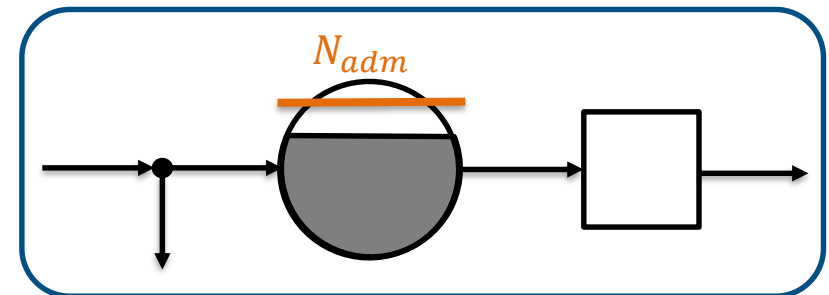


[10] Frigerio N. 2016. Optimal Stochastic Switching of Machine Tools in Energy Efficient Manufacturing Systems, PhD Thesis, Politecnico di Milano, Italy.

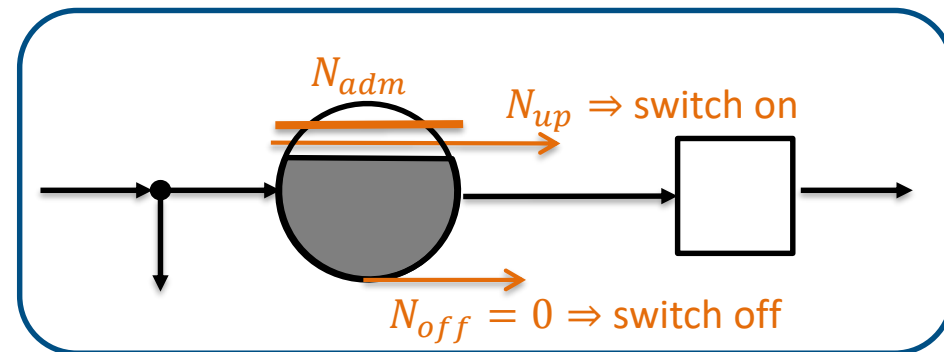
[11] Frigerio N., Shanthikumar J. G., Geng N., Matta A. Dynamic Programming for Machine Energy Control with Buffer Level Information, *under review for IISE Transaction*.

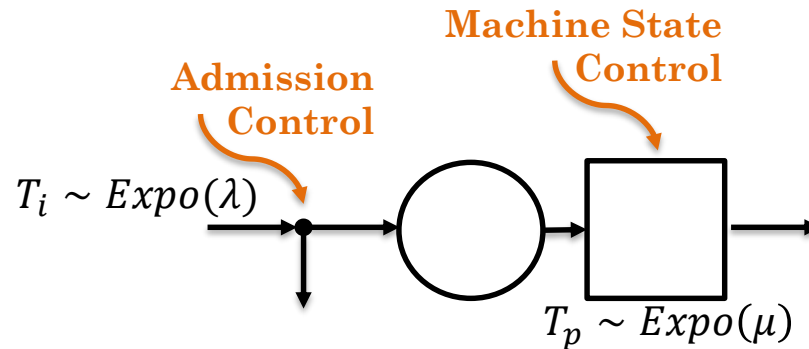
- 1) The development of a dynamic programming based model for the combined optimization problem of controlling machine state and part admission;
- 2) To analyze structural properties of the control such as (with $r > r_{\min}$):

- Exhaustive service;
- Parts are admitted up to threshold N_{adm} ;
- The machine is switched off when buffer is empty ($N_{off} = 0$), and it is switched on after N_{up} parts accumulates into the system.



OR





1. Perfectly reliable server;
2. Infinite downstream buffer;
3. Transitory (startup) durations are i.i.d. random variables $T_{\text{su}} \sim \text{Expo}(\gamma)$;
4. The startup is long enough to guarantee the quality of processed parts;
5. The random variables are not affected by the control;
6. The stochastic process are independent each other;
7. **Machine processing and startup cannot be interrupted by the control.**

The control problem can be modeled as **Discrete Time Markov Decision Process** problem with the **uniformization** technique (Lippman [15]):

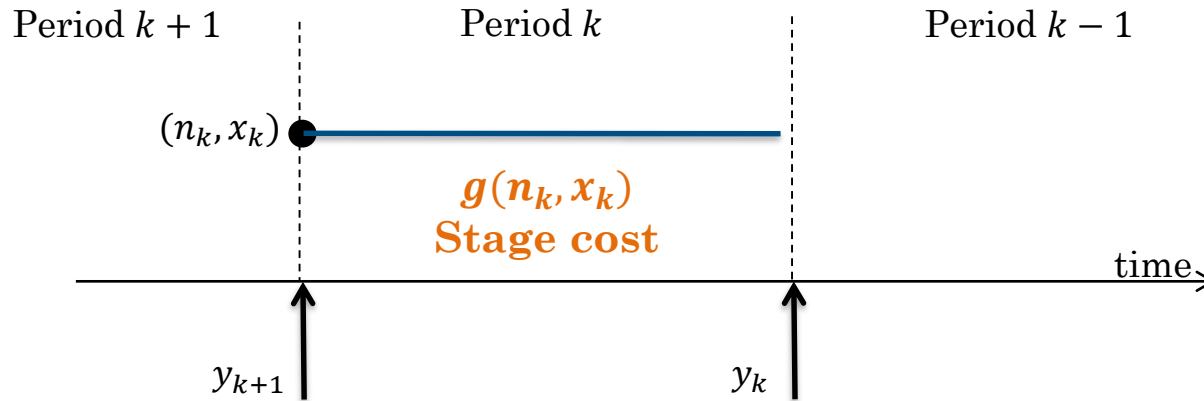
- A countable number of states;
- Random time between transitions;
- Observable system state;
- The feasible control action set depends on system state and event occurrence.

[11] S.A. Lippman. Applying a new device in the optimization of exponential queueing system. *Operation Research*, 23:687–710, 1975

[12] Powell, W. 2011. *Approximate Dynamic Programming*. 2nd ed. John Wiley & Sons, Inc., Hoboken, NJ, USA.

[13] Puterman, M. L. 1994. *Markov Decision Processes: discrete stochastic dynamic programming*. John Wiley & Sons, Inc., Hoboken, NJ, USA.

[14] Ross, S. 1983. *Introduction to stochastic dynamic programming*. Academic press, NY.



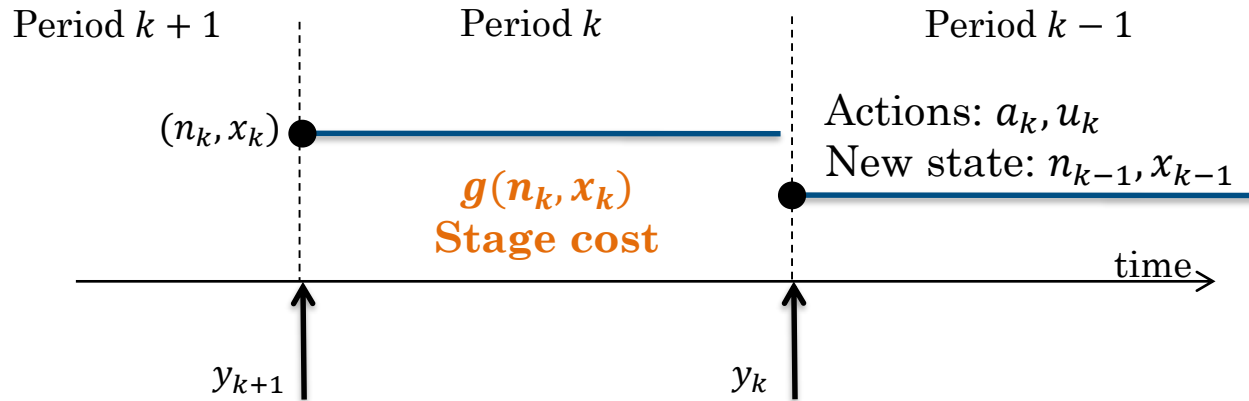
Denote a period k when k transitions are left.

Decision Epochs are the occurrences of event y_k at the end of period k :

$$y_k = \begin{cases} \text{A} - \text{part Arrival} \\ \text{D} - \text{part Departure} \\ \text{C} - \text{startup Completion} \end{cases}$$

System State (n_k, x_k) observed at the beginning of period k :

- n_k = number of parts in the system;
- x_k = machine state $x \in \{1,2,3,4\}$.



Control Actions $(a_k, u_k) \in A(n_k, x_k, y_k)$ that is the set of feasible actions depending on system state (n_k, x_k) and event instance y_k .
Actions are taken at the end of period k after the event is observed.

- Upon arrival, a part is admitted if $u_k = 1$, otherwise $u_k = 0$
- The machine state is controlled according to machine model with a_k
e.g. if $x_k = 1 \Rightarrow a_k \in \{1,3\}$

System Dynamics is assumed to be stationary.

System Dynamics

System dynamics is assumed to be stationary.

Given the current system state (n_k, x_k) the instance of event y_k , and the control actions (a_k, u_k) , the next system state (n_{k+1}, x_{k+1}) is as follows:

$$(n_{k+1}, x_{k+1}) = \mathbb{Z}(n_k, x_k, y_k, a_k, u_k)$$

$$(n_{k+1}, x_{k+1}) = \begin{cases} (n_k + u_k, a_k) & \text{if } y_k = \text{A} \\ (n_k - 1, a_k) & \text{if } y_k = \text{D} \\ (n_k, a_k) & \text{otherwise} \end{cases}$$

Where action a_k is in a feasible action set (Table 1).

Table 1 : Feasible action set

x	n	y	$\mathcal{A}_{s,y}$
1	$\forall n$	$A \vee \emptyset$	$\{1,3\}$
	$n > 0$	$A \vee \emptyset$	$\{1,2,4\}$
2	$n = 0$	A	$\{1,2,4\}$
		\emptyset	$\{1,2\}$
3	$n > 0$	$A \vee \emptyset$	$\{3\}$
	$n = 0$	C	$\{1,2,4\}$
4	$n > 1$	$A \vee \emptyset$	$\{4\}$
		D	$\{1,2,4\}$
4	$n = 1$	$A \vee \emptyset$	$\{4\}$
		D	$\{1,2\}$

The **infinite-horizon optimal discounted cost** is: $J = \sum_{k=1}^{\infty} \min_{a_k, u_k} \mathbf{E}[f(n_k x_k, a_k, u_k)]$

- Machine energy cost $c(x)$ where $c(4) > c(2) > c(1)$ and $c(3) > c(2)$;
- Inventory holding cost $h(n)$ where the convexity holds:

$$h(n+2) - h(n+1) \geq h(n+1) - h(n)$$

- Rejection cost $c_r(n) \geq 0$ when the part is rejected;
- Production reward $r \geq 0$ earned at process completion.
 - It represents the valuable reward for the production of each part;
 - It may be correlated to the downstream-system (as r increases, the control is prone to be more productive).

Given a discount rate α , $v_{k+1}^*(n_{k+1}, x_{k+1})$ denotes the discounted cost when $k+1$ transitions are left:

$$v_{k+1}^*(n_{k+1}, x_{k+1}) = g(n_{k+1}, x_{k+1}) + E_{(a_{k+1}, u_{k+1})}[v_k^*(n_k, x_k | n_{k+1}, x_{k+1})]$$

$$\lim_{k \rightarrow \infty} v_k^*(n, x) = v^*(n, x) = J$$

For example: $v_{k+1}^*(n, 4) \Big|_{n>1} =$

$\frac{h(n) + c(4)}{\eta}$
Stage Cost

Arrival	→	$+\frac{\lambda}{\eta} \min_{u=\{0,1\}} v_k^*(n + u, 4)$	Cost – To – Go
Departure	→	$+\frac{\mu}{\eta} \left[-r + \min_{a=\{1,2,4\}} v_k^*(n - 1, a) \right]$	
Uniformization term	→	$+\frac{\eta - \lambda - \mu - \alpha}{\eta} v_k^*(n, 4)$	

Note: $\eta = \lambda + \mu + \gamma + \alpha$

- Numerical data are obtained with value iteration algorithm in Matlab©:
 - 20'000 iterations (difference between iterations smaller than 0.1%)
 - Finite number of states: $n = 0, 1, \dots, 200$

The optimality of **threshold based** policies is shown.

The advantage of combined control is shown by comparing four policies:

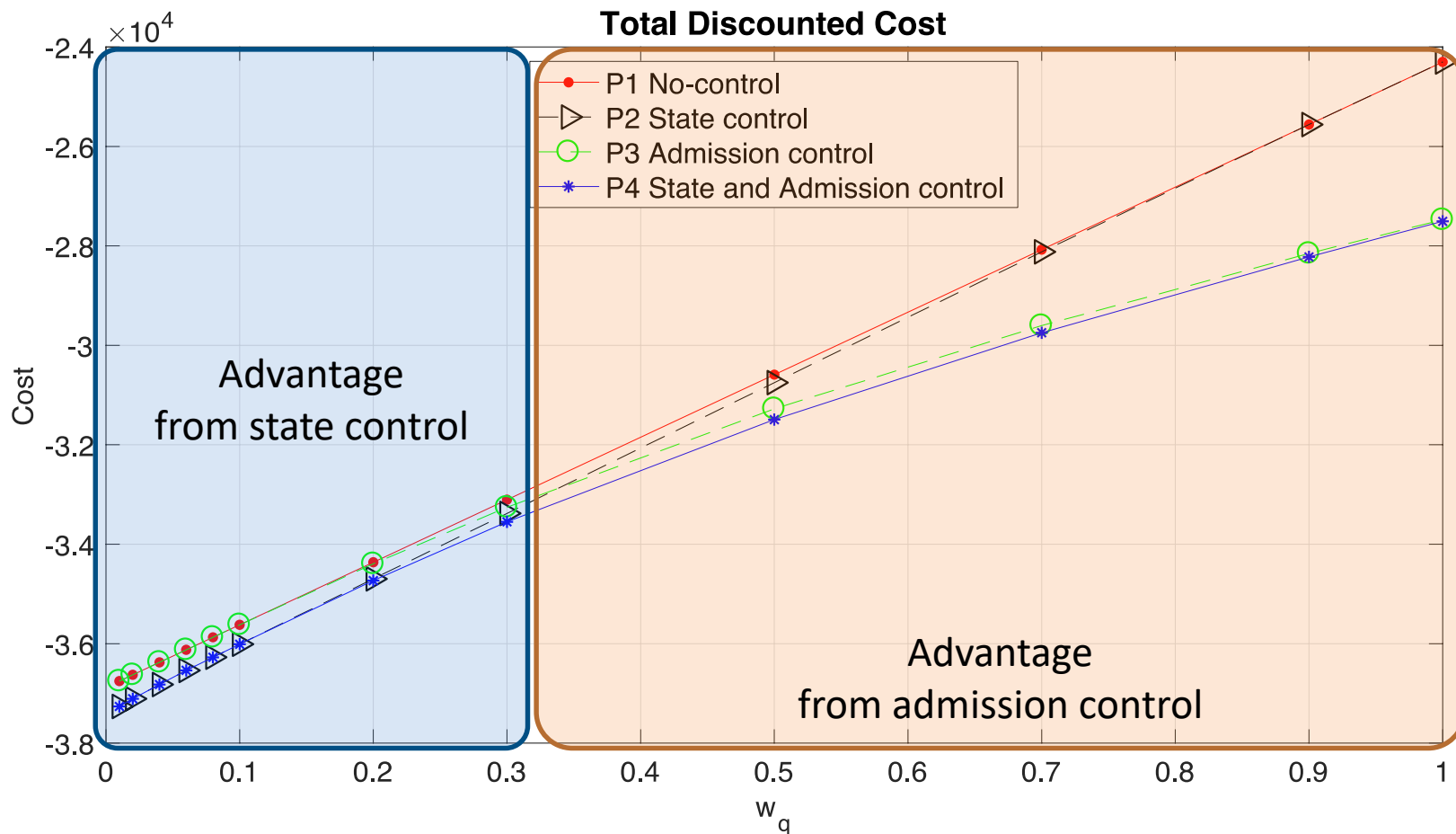
P1 – No control (admit all, machine no controlled)

P2 – Machine state control (admit all)

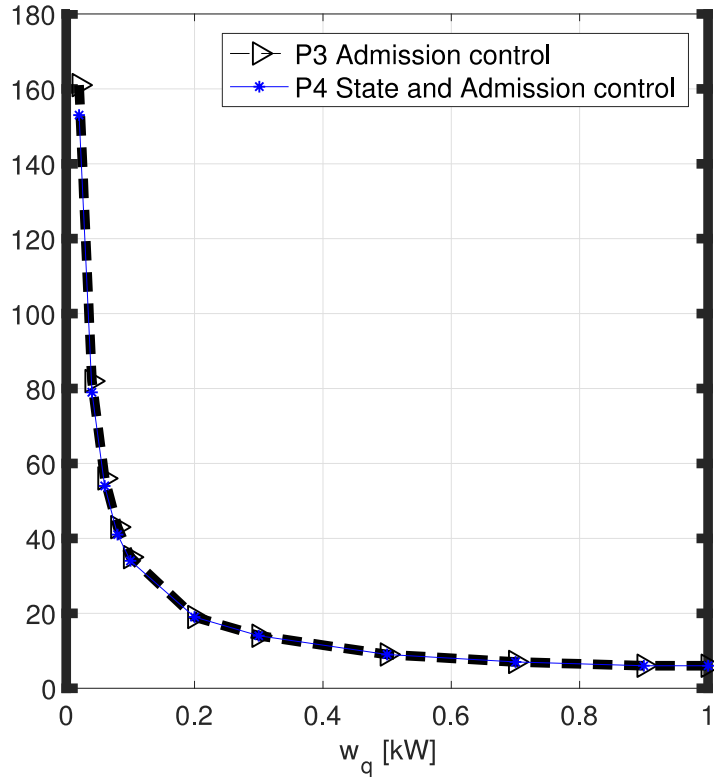
P3 – Admission control (machine no controlled)

P4 – Machine state control and admission control

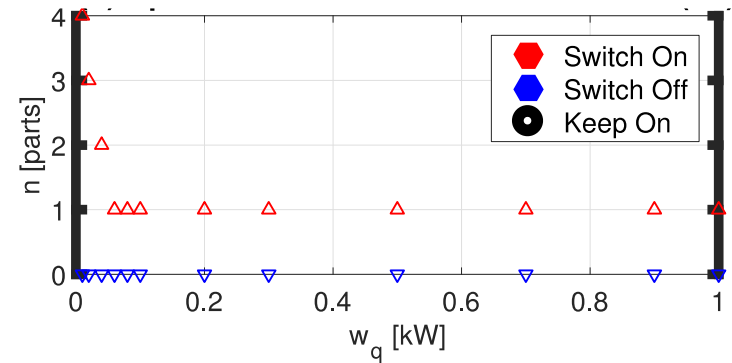
- Special case: $r < r_{min} \Rightarrow$ no production advantage (no admission / no production)
- Sensitivity analysis is performed. Detailed results for:
 - Holding cost $h(n) = w_q n$
 - Arrival rate λ



Admitted Parts



Machine Control (switch off/on)

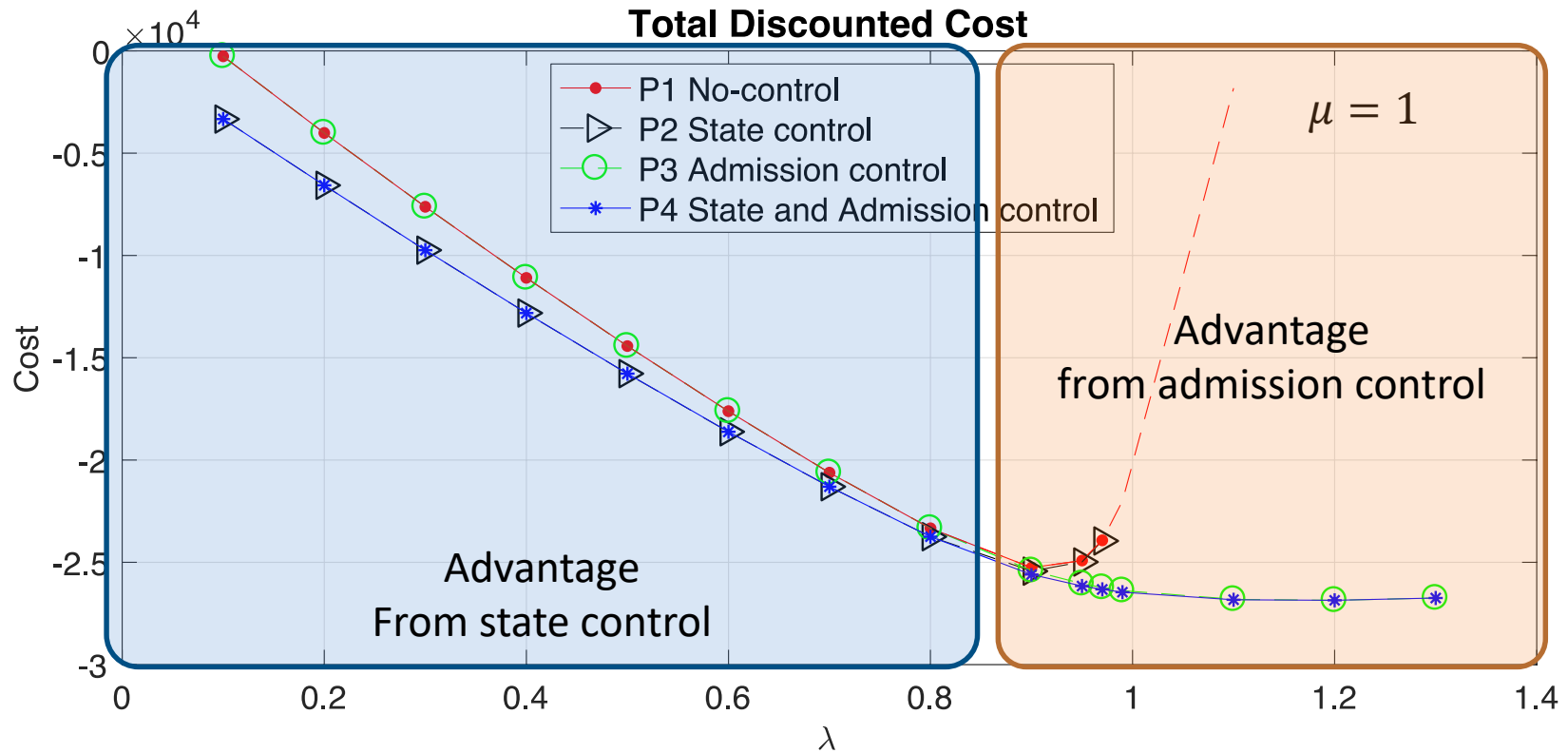


Numerical Analysis

Arrival Rate with $w_q > 0$

$c_{out} = 0$	$t_p = 1$
$c_{on} = 1$	$t_{su} = 0.23$
$c_{su} = 1.91$	$r = 15$
$c_{work} = 5.18$	$c_r = 0$
$w_q = 0.07$	$\alpha = 10^{-5}$

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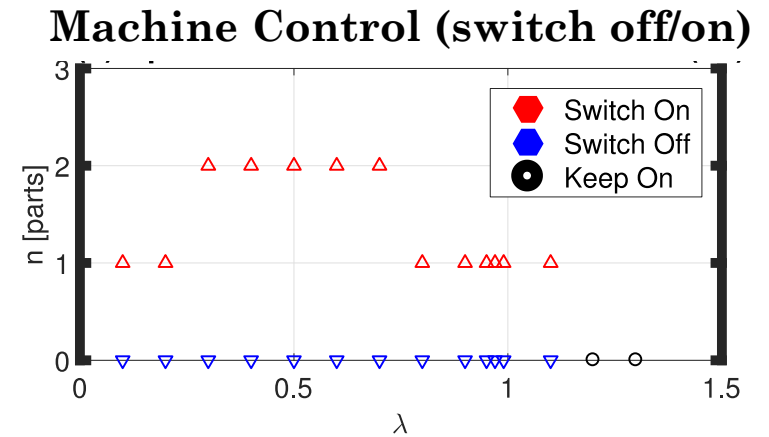
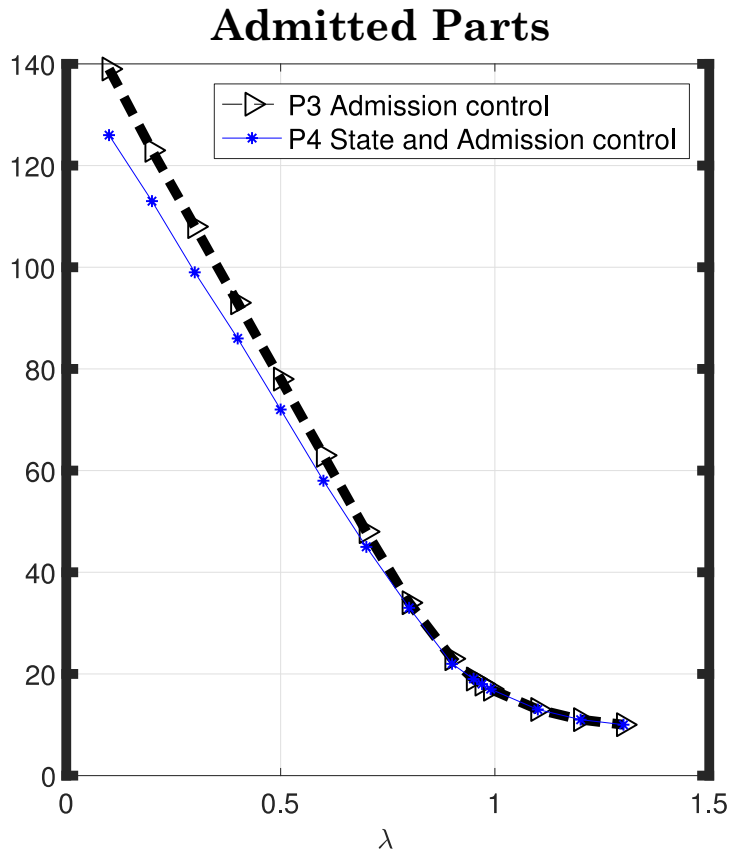
With $\lambda < 0.8$, savings are related to the machine control (switch off/on). For high utilization, savings are related to the admission control that limits the queue length.

Numerical Analysis

Arrival Rate with $w_q > 0$

$c_{out} = 0$	$t_p = 1$
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Numerical Analysis

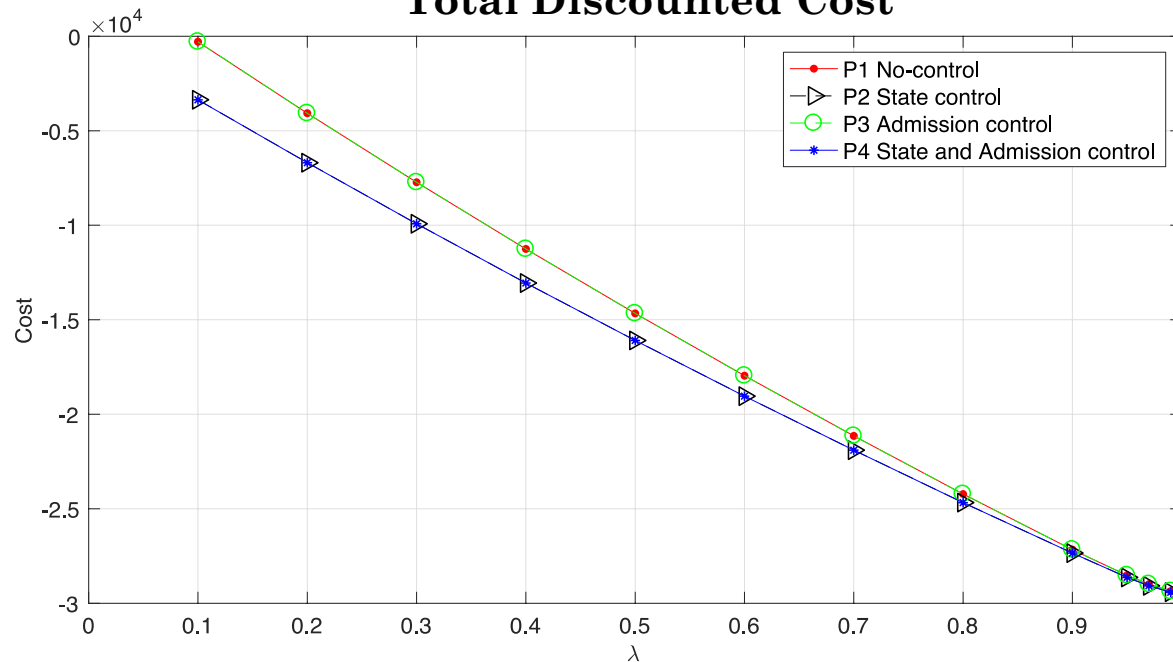
Arrival Rate with $w_q = 0$

$$\begin{aligned}
 c_{out} &= 0 & t_p &= 1 \\
 c_{on} &= 1 & t_{su} &= 0.23 \\
 c_{su} &= 1.91 & r &= 15 \\
 c_{work} &= 5.18 & c_r &= 0 \\
 w_q &= 0 & \alpha &= 10^{-5}
 \end{aligned}$$

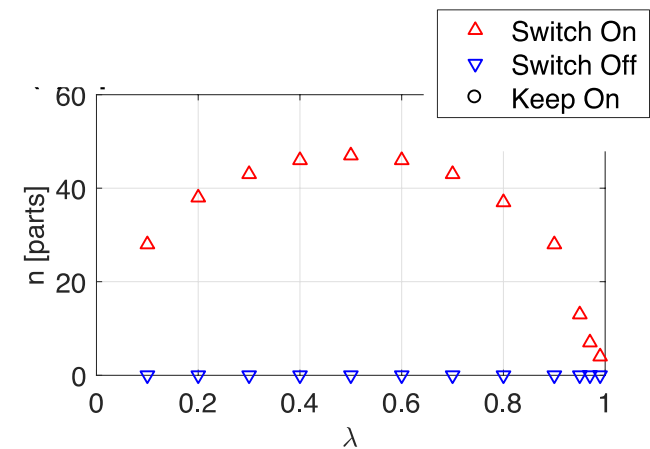
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➤ All parts are admitted

Total Discounted Cost



Machine Control (switch off/on)



- 1) A dynamic programming methodology has been used to model a machine tool with start/stop feature and requiring a startup, that is working in a production environment where the admission of parts is controlled.
- 2) Integration of productivity and sustainability criteria in the operation of manufacturing systems:
 - Structural property have been shown numerically;
 - Results are aligned with the common practice.
- a) Future results will be devoted to:
 - Prove analytically the results of this work;
 - Adding a control of machine service rate;
 - Multiple Machine “Sleeping” States.

Thank You for Your Attention

Any question or remark?

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- 1) Brundage, M.P., Q. Chang, Y. Li, G.X. Xiao, J. Arinez. 2014. Energy Efficiency Management of an Integrated Serial Production Line and HVAC System. *Automation Science and Engineering, IEEE Transactions on* 11(3) 789–797.
- 2) Chang, Q., G. Xiao, S. Biller, L. Li. 2013. Energy Saving Opportunity Analysis of Automotive Serial Production Systems (March 2012). *Automation Science and Engineering, IEEE Transactions on* 10(2) 334–342.
- 3) Doshi, B. T. 1986. Queueing systems with vacations— A survey.
- 4) Frigerio, N., A. Matta. 2016. Analysis on Energy Efficient Switching of Machine Tool With Stochastic Arrivals and Buffer Information. *Automation Science and Engineering, IEEE Transactions on* 13(1) 238–246.
- 5) Jia, Z., L. Zhang, J. Arinez, G. Xiao. 2015. Performance Analysis of Bernoulli Serial Production Lines with Switch-On/Off Machine Control. *Proceedings of the IEEE Conference of Automation Science and Engineerings.*
- 6) Ke, J.C., C.H. Wu, Z.G. Zhang. 2010. Recent Developments in Vacation Queueing Models: A Short Survey. *Journal of Operation Research* 7(4) 3–8.
- 7) Lippman, S.A. 1975. Applying a new device in the optimization of exponential queueing system. *Operation Research* 23 687–710.

- 8) Mashaei, M., B. Lennartson. 2013. Energy Reduction in a Pallet-Constrained Flow Shop Through On – Off Control of Idle Machines. Automation Science and Engineering, IEEE Transactions on 10(1) 45–56.
- 9) Powell, W. 2011. Approximate Dynamic Programming. 2nd ed. John Wiley & Sons, Inc., Hoboken, NJ,USA.
- 10) Puterman, M. L. 1994. Markov Decision Processes: discrete stochastic dynamic programming. John Wiley & Sons, Inc., Hoboken, NJ, USA.
- 11) Ross, S. 1983. Introduction to stochastic dynamic programming. Academic press, NY.
- 12) Serfozo, R. 1979. An Equivalence between Continuous and Discrete Time Markov Decision Processes. Operations Research 27(3) 616–620.
- 13) Serfozo, Richard. 1981. Optimal control of random walks, birth and death processes, and queues. Advances in Applied Probability 13(1) 61–83. URL
- 14) Stidham, S., R. Weber. 1973. A survey of markov decision models for control of networks of queues. Queueing Systems 13(1) 291–314.
- 15) Tadj, L., G. Choudhury. 2005. Optimal Design and Control of Queues. TOP 13(1) 359–412.
- 16) Takagi, H. 1991. Queueing analysis: a foundation of performance evaluation, Vacation and priority systems,Vol.1, Part I, Amsterdam,.
- 17) Tian, N., Z.G. Zhang. 2006. Vacation Queueing Models – Theory and Applications. Springer, New York.